A Segment-Based Multipath Distribution Method in Partially-Trusted Relay Quantum Networks

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ABSTRACT

As a promising application of quantum information technology, Quantum Key Distribution (QKD) can provide information-theoretically secure key exchange for adjacent communication parties. To achieve long-distance secure communication and scale expansion against inherent channel loss, trusted relays, which are assumed to be absolutely secure, are introduced into QKD networks. However, in practice, trusted relays may be compromised by attacks from ubiquitous eavesdroppers even protected by powerful hardware. Thus, how to ensure the security of end-to-end key distribution in partially-trusted relay QKD networks with the coexistence of trusted relays and untrusted relays becomes a challenging but urgent problem to be solved. To address this critical problem, in this article, we design a segment-based multipath key distribution method. The basic idea of the method is to maximize the security of the end-to-end key distribution through the segment-based multipath key distribution. Under the premise of security level requirements, we further propose a flexible key reconstruction scheme to improve the efficiency of key distribution and obtain available secret keys as many as possible. The extensive simulations are conducted and the results reveal that our method significantly outperforms the traditional multipath QKD method in terms of both security and efficiency.

INTRODUCTION

In the digital era, information security is always an essential and indispensable issue for various applications. Classical cryptography has been developed for decades to guarantee network communication security, and numerous cryptographic algorithms have been successfully applied. For example, Rivest-Shamir-Adleman (RSA), one of the most famous public-key encryption schemes, has been widely used in key agreement and authentication. However, since the security of most public-key ciphers is based on the difficulty of factoring integers or the discrete logarithm problem in mathematics, the upcoming quantum computers, which own exponentially increasing computational power, have posed a fatal threat to conventional cryptography by using quantum algorithms, such as Shor’s algorithm [1, 2]. Therefore, it is necessary to find a powerful method to fight against the security problem caused by quantum computing.

As a promising technology that provides anti-quantum computing security, Quantum Key Distribution (QKD) allows two communicating parties to share secure keys by sending and measuring quantum bits, that is, qubits. The no-cloning theorem proves that an arbitrary unknown qubit cannot be cloned losslessly [3]. Thus, it is impossible for eavesdroppers to copy the qubits without being detected successfully, and guarantees information-theoretically secure key exchange. At present, qubits are usually achieved by photons and propagated through optical fibers or free space. There are 428 km, 509 km, 511 km, and 833 km QKD experiments in recent several years, there has been satellite to ground QKD using BB84, and BBM92 for free space QKD, and the integrated QKD network [4, 5].

Considering the inevitable photon loss and decoherence in quantum channels, trusted relay is a practical approach to extend the distance of QKD [6, 7]. Trusted relay works by using One-Time-Pad (OTP) technique to achieve end-to-end key distribution between two distant communication parties in a hop-by-hop manner. Due to its flexibility, simplicity, and scalability, trusted relay has been widely used in cutting-edge QKD networks and significantly facilitates the construction of long-haul trunk QKD [5, 8]. However, the security of key distribution process relies on the security assumption of trusted relays, that is, eavesdroppers cannot compromise trusted relays. Unfortunately, some operations of trusted relays, including key storage, encryption, and decryption, are implemented in classical computers, which makes it possible for eavesdroppers to attack. Therefore, in the current QKD networks, the insecurity of some relay nodes must be considered, which is conducive to breaking the assumption that relays are completely trusted and further improving the security of the whole system. Hence, how to achieve end-to-end key distribution in the partially-trusted relay QKD networks becomes a critical and urgent problem to be solved.
To address the security problem caused by untrusted relays, most existing studies mainly consider Measurement-Device-Independent (MDI) QKD [9] and multipath key distribution method [10, 11]. The former can expand the distribution distance and close all detection loopholes with the aid of a measurement node that can even be untrusted. However, its requirement for the location of the measurement node makes it unable to solve the situation that two untrusted relays are adjacent and limit its application. The latter can effectively improve security by simultaneously distributing secret keys through multiple disjoint paths with the help of secret sharing. Unfortunately, some drawbacks of the existing multipath key distribution method still hinder its practical applications: First, in practical network topologies, the number of disjoint paths required by the multipath key distribution method is limited. Second, for a partially-trusted relay QKD network, the existing multipath key distribution method can hardly utilize the location information of trusted relays for routing to further improve the security of end-to-end key distribution. Besides, considering that different fields including military, financial, and government have different security level requirements for secret keys, a dynamic secret sharing scheme is further required to achieve flexible key reconstruction.

To correspond to the above drawbacks and achieve secure and efficient key distribution in the partially-trusted relay QKD networks, in this article, we analyze the influence of different paths on the security of key distribution by using a probability model and then propose a novel segment-based multipath key distribution method that utilizes the location information of trusted relays to maximize the security of the end-to-end key distribution. After that, we further propose a flexible key reconstruction scheme, which can adjust the key reconstruction process to achieve higher distribution efficiency under the premise of meeting various security level requirements. The main contributions of our work are summarized as follows:

1. To tackle the security problem in the partially-trusted relay QKD networks, we propose a segment-based multipath key distribution method, which can fully utilize the location information of trusted relays and achieve as high security as possible in the process of end-to-end key distribution. It overcomes the drawbacks of the existing schemes.
2. Considering the diverse security requirements of applications, we further propose a flexible key reconstruction scheme. Based on the successfully distributed secret keys on the paths of each segment, this post-processing procedure can significantly improve the efficiency of key distribution between arbitrary communicating parties under the premise of meeting various security level requirements.
3. To evaluate the performance of the proposed key distribution method, we conduct extensive simulations in different scenarios. Results show that the proposed method significantly outperforms the traditional multipath method for security and efficiency.

The next section introduces the background, network model, and security problem considered in this article. After that, we describe the specific details of the segment-based multipath method. We conduct simulations and analyze the results following that. Finally, we conclude this work and envision future directions.

**Background and Problem Statement**

**Background**

Currently, various QKD protocols have been proposed and demonstrated experimentally, including Bennett-Brassard-1984 (BB84), Ekert-91 (E91), and Measurement-Device-Independent QKD (MDI-QKD) [12], and so on. Here, we take the prepare-and-measure protocol BB84 as an example to clarify the specific implementation procedure of QKD and further introduce the working process of long-distance key distribution and multipath key distribution.

**Point-to-point QKD:** As shown in Fig. 1, Alice and Bob are two communicating parties who want to share secret keys, and they are connected by a quantum channel and a classical channel. Alice sends qubits to Bob, and each qubit is determined by two random classical bits, one for the encoding basis and another for the bit (0 or 1) to send. Bob receives and measures the qubits with random bases and tells Alice which qubits he received. Then, they exchange the bases they chose via a classical channel and only keep the measurement results of the same bases in the sifting. Part of the reserved bits are used for eavesdropping detection, and the remaining part will become the shared keys after error correction and privacy amplification.

**Long-Distance QKD:** Long-distance QKD can be achieved in a hop-by-hop manner to break the distance limitation by deploying relays between two distant nodes [13]. As shown in Fig. 1, node A takes $K_1$ as the secret key; node B encrypts $K_1$ with $K_2$, that is, $E_{K_2}(K_1)$ and sends it to node C; node C decrypts and sends it to node D in the same way. Finally, node D gets $K_1$. At this time, a global key $K_1$ is shared between node A and node D.

**Multipath QKD:** In the partially-trusted relay QKD networks, distributing global keys through one path may lead to key leakage under the attack of eavesdroppers. As shown in Fig. 2, node A and node E distribute keys through two disjoint paths with the help of secret sharing. Unfortu-

![FIGURE 1. The illustration of point-to-point QKD and long-distance QKD.](image)
FIGURE 2. A typical structure of a partially-trusted relay QKD network. In order to ensure the security of the global key, two paths are used for key distribution. The final key is reconstructed from the keys distributed by the two paths.

To highlight the security problem in the partially-trusted relay QKD networks, in the following, we give the definition of two kinds of relays in the network and introduce the adversary model considered in this article.

**Adversary Model:** Since secret keys are transformed from ciphertext into plaintext on each relay during the end-to-end key distribution process, eavesdroppers pay more attention to compromising the relays. Each untrusted relay has a security probability to indicate that it has not been successfully attacked. The eavesdropper can arbitrarily select relay nodes to attack, but it can only obtain the key information of the successfully attacked relay. For an end-to-end key distribution, the key information will only be transmitted once on each relay node. Similarly, we adopt a probability model to evaluate the security of end-to-end key distribution. For single-path key distribution, the security probability of key is the probability that all relay nodes on the path successfully resist eavesdropping. For multopath key distribution, the security probability is the probability that at least one path is secure.

**Problem Statement**

Currently, many QKD networks have been deployed and used in business, and they are mainly based on the trusted relay technique. The insecurity of partial relay nodes in large-scale networks cannot be ignored. Meanwhile, the consideration of untrusted relays can break the assumption that relay nodes must be completely trusted and improve the security of the whole network. Therefore, the problem of secure key distribution must be solved in the partially-trusted relay QKD networks.

As an effective solution to protect the security of the key distribution process in the partially-trusted relay QKD networks, there are some existing studies that focus on multipath QKD in quantum networks with untrusted relays. Their security analysis of the process of key distribution can be divided into two categories: network connectivity [10] and probabilistic [11, 14]. The former usually proposes a scheme that can tolerate a certain number of compromised nodes for secure transmissions. The latter usually analyze the security of the key distribution according to the security probability of the untrusted relays and the paths for key distribution. However, these studies, on the one hand, neglect the impact of key distribution path selection but pay more attention to the number of paths. On the other hand, they ignore users’ various security requirements. Hence, in the next section, to improve the security of key distribution and balance the security and efficiency of key distribution, we design a segment-based multipath key distribution method and a flexible key reconstruction scheme.
SEGMENT-BASED MULTIPATH KEY DISTRIBUTION

Overview

As a secret key distribution platform, QKD networks supply quantum keys for various fields, for example, military, finance, and government. To address the potential threats of eavesdropping on immediate relays in the partially-trusted relay QKD networks, we design a novel segment-based multipath key distribution method. Different from the traditional multipath distribution scheme, the proposed method splits the end-to-end distribution process into segments, improving the security of key distribution. In addition, considering various requests in QKD networks have different security requirements for keys, we propose a flexible key reconstruction scheme to adjust the security and efficiency in the end-to-end key distribution. The overall workflow of the method is shown in Fig. 3.

SEGMENT-BASED KEY DISTRIBUTION METHOD

In the segment-based multipath key distribution, the distribution process is divided into two stages, that is, key distribution within segment and end-to-end distribution. The specific illustration is shown in Fig. 4. After receiving a request, the centralized server determines the routing paths and key reconstruction strategy according to the network status and security requirement, and then sends results to relays in the network. After that, the key distribution within the segment is performed, and each corresponding path is used for key distribution. The obtained keys are shared by the trusted relay nodes at both ends of the segment, and then they are reconstructed into new keys as required. Next, these physically non-adjacent but logically adjacent trusted relays share the reconstruction keys with each other and use these keys to achieve the end-to-end key distribution in a hop-by-hop manner. The security probability of the end-to-end global key is the product of the security probabilities of reconstructed keys on each segment. Under the same distribution paths, the segment-based distribution method can improve the security of the final global keys more than the non-segmented distribution method. The basic idea is that when a relay node is eavesdropped successfully, compared with the non-segmented multipath distribution, only the key on the segmented path where the relay node is located will be leaked, rather than the key on the whole path from the source node to the destination node.

Finding appropriate segmented paths is indispensable in the network. Various routing algorithms proposed for classical networks cannot be directly applied to the partially-trusted relay QKD networks because they do not consider the security of key distribution. Consumption of local keys for long-distance QKD increases with the increase of hops, which makes it necessary for routing to consider resource consumption. Besides, we can make full use of the location information of trusted relays to find more secure paths in the partially-trusted relay QKD networks.

To find more resource-saving and secure paths, we define the expected security probability $E_{sp}$ as the routing metric to quantify a path, it equals the product of the security probability of each relay on the path. A larger value not only means that the path is safer but also usually means that the path is shorter. The classical Dijkstra algorithm can find the shortest path because the routing metric is additive, which means that the cost of the path is the sum of the costs of all edges on the path. However, our metric is multiplicative and monotonically decreasing. For the non-additive but monotonic routing metric $E_{sp}$, we apply it to the classical Dijkstra algorithm and call it ExDijkstra to find the path between source and destination with the maximum evaluation value.

In the previous work, the paths for multipath key distribution are usually node-disjoint (i.e., one relay can only be used in one path) to ensure an untrusted relay can only get one key. However, this strategy not only finds limited paths but also finds more scattered and long paths, which wastes more local keys and increases the risk of key leakage. Thus, we not only use the trusted relays to segment the paths but also allow multiple paths crossing on trusted relay to reduce the average length of paths.

We propose a heuristic Segment-based Multipath Routing (SMR) algorithm to find appropriate paths for maximizing the security of key distribution. The steps shown in Fig. 3 are described as follows:

- Find trusted relays for segment: SMR finds the segment nodes between the source

FIGURE 4. The illustration of the segment-based multipath key distribution method, two segments reconstruct keys respectively and then distribute the global key in a hop-by-hop manner.
node $s$ and the destination node $d$ through an iterative process. In the beginning, the segment node set is empty. Each time, the classical Dijkstra is used to find the trusted relay node $r$ with the minimum sum of the distances $s$ and $d$, and then the ExDijkstra is used to find two non-segmented paths from $s$ to $d$ and two segmented paths from $s$ to $r$ and $r$ to $d$. Judge whether the security probability of segment-based distribution is greater than that of non-segmented distribution. If yes, add $r$ to the segment node set and set $r$ as new $s$ to continue the iterative process, otherwise, the iterative process will end.

- Find segment-based multiple paths: Based on the segment node set in the previous step, each time, ExDijkstra is used to find a path for each segment, the found paths will be deleted on the topology. The algorithm stops when no more paths can be found.

**Flexible Key Reconstruction**

In the existing multipath schemes, the keys distributed on different paths are reconstructed into a global key via XOR operation. In this case, the security of the key is undoubtedly the strongest, but the security gain brought by the increase in the number of paths has a marginal utility. Besides, considering that different requests have different requirements for the security of the key, we propose a flexible key reconstruction scheme, which can offer a dynamic reconstruction process. The basic idea is adjusting the number of keys consumed by the reconstruction on the premise of meeting the requirements of the security to improve the efficiency of end-to-end key distribution.

In the partially-trusted relay QKD networks, a key request includes source node, destination node, and key security level requirement $\epsilon$ represented by security probability. SMR will find multiple paths that cross over trusted relays between source node and destination node. These paths are divided into multiple segments by some trusted relays, and each path of each segment performs key distribution respectively before key reconstruction.

Before actual end-to-end distribution, we need to decide how to match the reconstructed keys between segments and how to achieve the key reconstruction on each segment. The reconstructed keys on each segment have different security probabilities, in order to make as many global keys as possible meet the security level, we use a balanced matching strategy to improve the minimum security probability of global keys.

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**Performance Evaluation**

**Simulation Setup**

To verify the performance of the SMR algorithm, we use numerical simulation compare it with the existing Multiple Stochastic Paths (MSP) algorithm.
nodes, the end-to-end security probability is also
with the increase in the number of trusted relay
Figure 6a, as the security probability of untrusted relays
to different routing algorithms. As shown in Fig.
apply the proposed key reconstruction scheme
total number of keys. The key length represents the
ciency in the process of key distribution. We use
and shorter paths, SMR always consumes fewer
rless users’ diverse security level requirements,
in the number of trusted relays, which consumes more
obtain a higher security rate. As shown in Fig. 6b,
sm can still obtain the advantage of key length and have a more obvious improvement.

Conclusions and Future Directions
In this article, we studied the potential eavesdropping attacks on immediate relays existing in the partially-trusted relay QKD networks and analyzed the impact of key distribution paths on the security of the end-to-end key distribution process. To overcome the drawbacks of the existing work and address this security problem, we designed a segment-based multipath key distribution method by utilizing the location information of trusted relays to maximize the security of the key distribution process. In addition, we further proposed a flexible key reconstruction scheme to reconstruct secret keys for numerous demands while still satisfying users’ diverse security level requirements, and thus the efficiency of key distribution can be further enhanced. Extensive simulations have been conducted, and the results show that the proposed method significantly outperforms the traditional multipath key distribution method in terms of security, resource consumption, and distribution efficiency. In the future, we plan to further investigate the impact of the number and the location of trusted relays in the network and provide an optimized trusted relay deployment strategy.

With the continuous development of quantum information technology, the quantum Internet will eventually be established and support quantum computers and quantum communication [15]. As a significant application in quantum Internet, QKD provides unconditionally secure keys for classical networks. However, attacks against relay nodes emerge endlessly, which greatly affects the security of long-distance QKD. The results show that our method can effectively improve the security of key distribution, which provides assistance for building the future large-scale quantum network.

In terms of resource consumption, because our proposed routing algorithm makes full use of trusted relay nodes, more paths can be found with the increase in the number of trusted relays, which consumes more resources and obtains a higher security rate.

Figure 6. The impact of different number of trusted relay nodes: a) End-to-end security probability and key consumption rate; b) Length of the global key. The security probability of untrusted relay nodes is set to 0.8.
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REFERENCES


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